

key Energy and Chemical Reactions

CALORIMETRY

Measuring heat (formerly measured in calories) is called **calorimetry**. Now we measure heat energy in Joules (J). The equation we use is:

$$q = m \cdot C \cdot \Delta T$$

q = heat energy

m = mass of water

C = the specific heat capacity

ΔT = the change in temperature (in °C or K)

ΔT

1. Water has a specific heat capacity of 4.184 J/g·°C.

This means it takes 4.184 J to heat 1.00 gram of water 1.00°C.

- a) How much energy will it take to heat 10.0 grams of water 1°C? 41.84 J
b) How much energy is needed to heat 30.0 g H₂O from 10.0 °C to 50.0 °C? 5020 J

$$q = (4.184 \text{ J/g}^\circ\text{C}) (30.0 \text{ g}) (50 - 10)$$

2. Let's try a standard **calorimetry** problem.

A pot of water (2.5 Liters of water) initially at 25.0°C is heated to boiling (100.°C).

How much energy (in J) is needed to heat the water? (The density of water is 1 g/mL.)

$$2.5 \text{ L} = 2500 \text{ g}$$

$$= 1000 \text{ g/L}$$

$$q = (2500 \text{ g}) (4.184) (100 - 25)$$
$$q = 784500 \text{ J} \rightarrow 7.8 \times 10^5 \text{ J}$$

What would this amount of heat be in kJ? $7.8 \times 10^2 \text{ kJ}$

$$\frac{7.8 \times 10^5 \text{ J}}{1000 \text{ J}} = 7.8 \times 10^2 \text{ kJ}$$

3. What amount of heat is *released* when 175 g of water *cools* from 100.°C to room temperature, 20.0 °C?

$$q = (175 \text{ g}) (4.184) (20 - 100)$$

$$q = -58600 \text{ J}$$

4. We don't always have to warm up or cool down water. The specific heat capacity of copper metal is 0.39 J/g·°C. It is easier (easier/more difficult) to heat up copper than to heat up water.

How much energy would it take to heat up a 5.20 g sample of copper from 20.0 °C to 100.°C?

$$q = (5.20 \text{ g}) (0.39 \text{ J/g}^\circ\text{C}) (100 - 20)$$

$$q = 162 \text{ J}$$

5. If 300. J of heat energy were used to heat up a 5.00 gram sample of copper metal and a 5.00 gram sample of water both starting at 10.0°C, calculate the final temperature of each sample?

copper

$$300. \text{ J} = (5.00) (0.39) (x - 10)$$
$$x = 163^\circ\text{C}$$

water

$$300. \text{ J} = (5.00) (4.184) (x - 10)$$
$$x = 24.3^\circ\text{C}$$

Signs of DT and q:

- q means heat is released. + q means heat is absorbed.

DT is always *final* temperature - *initial* temperature.

If something is getting **hotter** (10° @ 30°) the DT is 30 - 10 = + 20°. (heat is absorbed)

If something is getting **cooler** (75° @ 25°) the DT is 25 - 75 = - 50°. (heat is released)

6. Suppose we mix 90.0 grams of hot water (90.0°C) with 10.0 grams of cold water (10.0°C).
Let x = the final temperature. C = 4.184 J/g·°C

a. Set up an expression for the energy *released* (q) by the hot water ($Dq_{\text{hot}} = m_{\text{hot}} CDT_{\text{hot}}$)

$$q = (90.0\text{g})(4.184)(x - 90)$$

b. Set up an expression for the energy *absorbed* (q) by the cold water ($Dq_{\text{cold}} = m_{\text{cold}} CDT_{\text{cold}}$)

$$q = (10.0\text{g})(4.184)(x - 10)$$

c. Knowing that the heat released = - heat absorbed, combine the two expressions and solve for x.

$$\begin{aligned} - (90.0\text{g} \cdot 4.184 \cdot (x - 90)) &= (10.0\text{g})(4.184)(x - 10) \\ - 376.56x + 3380.4 &= 41.84x - 418.4 \\ - 418.4x &= -34308.8 \end{aligned} \quad \boxed{x = 82^\circ\text{C}}$$

7. We don't always have to use water. Let's use some aluminum shot.

"shot" are these little pellets.

175 grams of hot aluminum (100.°C) is dropped into an insulated cup that contains 40.0 mL of ice cold water (0.0°C). Follow the example above to determine the final temperature, x.

a. Set up an expression for the heat lost by the aluminum (C=0.900 J/g·°C)

$$q = (175\text{g})(0.900\text{J/g}\cdot^\circ\text{C})(x - 100)$$

b. Set up an expression for the heat gained by the cold water.

$$q = (40.0\text{g})(4.184\text{J/g}\cdot^\circ\text{C})(x - 0)$$

c. Put the two expressions together (don't forget to change one of the signs) and solve for x.

$$\begin{aligned} - (175\text{g} \cdot 0.900 \cdot (x - 100)) &= 40.0\text{g} \cdot 4.184 (x - 0) \\ - 157.5x + 15750 &= 167.36x \\ \boxed{x = 48.5^\circ\text{C}} \end{aligned}$$

8. **Somewhat Confusing Definitions:** *→ look at the units to figure out calculation →*

There are several terms used in this chapter that sound very similar. Use the data provided to calculate each of them to clarify the differences. I've added some "Notes" that I hope will help.

74.8 J of heat is required to raise the temperature of 18.69 g of silver from 10.0°C to 27.0°C.

a. What is the **heat capacity** of the silver sample? (J/°C)

Note: This is a useful value only for this specific sample of silver.

$$\frac{q}{\Delta T} = \frac{74.8 \text{ J}}{27.0 - 10.0} = 4.40 \text{ J/}^\circ\text{C}$$

b. What is the **specific heat capacity** of silver? (J/g·°C)

Note: This is a useful value for **any** sample of silver that is heated or cooled. This is equivalent to the 4.184 J·g⁻¹·°C⁻¹ that we use for water. This value is also called the **specific heat**.

$$q = mc\Delta T$$
$$74.8 \text{ J} = (18.69 \text{ g})(c)(27.0 - 10.0^\circ\text{C})$$
$$c = 0.235 \text{ J/g}^\circ\text{C}$$